

**AP EAMCET Mathematics Previous Questions with Key – Test 6**

1) If  $f: \mathbb{R} \rightarrow \mathbb{R}$  is defined by  $f(x) = [2x] - 2[x]$  for  $x \in \mathbb{R}$ , then the range of  $f$  is (Here  $[x]$  denotes the greatest integer not exceeding  $x$ )

- 1)  $\mathbb{Z}$ , the set of all integers
- 2)  $\mathbb{N}$ , the set of all natural numbers
- 3)  $\mathbb{R}$ , the set of all real numbers
- 4)  $\{0,1\}$

2) Given that  $a, b$  and  $c$  are real numbers such that  $b^2 = 4ac$  and  $a > 0$ . The maximal possible set  $D \subseteq \mathbb{R}$  on which the function  $f: D \rightarrow \mathbb{R}$  given by  $f(x) = \log\{ax^3 + (a+b)x^2 + (b+c)x + c\}$  is defined, is

- 1)  $\mathbb{R} - \left\{-\frac{b}{2a}\right\}$
- 2)  $\mathbb{R} - \left(\left\{-\frac{b}{2a}\right\} \cup (-\infty, -1)\right)$
- 3)  $\mathbb{R} - \left(\left\{-\frac{b}{2a}\right\} \cup \{x: x \geq 1\}\right)$
- 4)  $\mathbb{R} - \left(\left\{-\frac{b}{2a}\right\} \cup (-\infty, -1)\right)$

3) For any natural number  $n$ ,  $(15 \times 5^{2n}) + (2 \times 2^{3n})$  is divisible by

- 1) 7
- 2) 11
- 3) 13
- 4) 17

4) For the matrix  $A = \begin{bmatrix} 3 & -3 & 4 \\ 2 & -3 & 4 \\ 0 & -1 & 1 \end{bmatrix}$ ,  $A^{-1} =$

1) A

2)  $A^2$

3)  $A^3$

4)  $A^4$

5) If  $A = \begin{bmatrix} k/2 & 0 & 0 \\ 0 & l/3 & 0 \\ 0 & 0 & m/4 \end{bmatrix}$  and  $A^{-1} = \begin{bmatrix} 1/2 & 0 & 0 \\ 0 & 1/3 & 0 \\ 0 & 0 & 1/4 \end{bmatrix}$  then  $k + l + m =$

1) 1

2) 9

3) 14

4) 29

6) If A and B are the two real values of k for which the system of equations  $x + 2y + z = 1$ ,  $x + 3y + 4z = k$ ,  $x + 5y + 10z = k^2$  is consistent, then  $A + B =$

1) 3

2) 4

3) 5

4) 7

7) Let  $z = x + iy$  and a point P represent  $z$  in the Argand plane. If the real part of  $\frac{z-1}{z+i}$  is 1, then a point that lies on the locus of P is

- 1) (2016, 2017)
- 2) (-2016, 2017)
- 3) (-2016, -2017)
- 4) (2016, -2017)

8) If  $13e^{i \tan^{-1} \frac{5}{12}} = a + ib$ , then the ordered pair (a, b) =

- 1) (12, 5)
- 2) (5, 12)
- 3) (24, 10)
- 4) (10, 24)

9) If  $z_1 = 1 - 2i$ ;  $z_2 = 1 + i$  and  $z_3 = 3 + 4i$ , then  $\left(\frac{1}{z_1} + \frac{3}{z_2}\right) \frac{z_3}{z_2} =$

- 1)  $13 - 6i$
- 2)  $13 - 3i$
- 3)  $6 - \frac{13}{2}i$
- 4)  $\frac{13}{2} - 3i$

10) If  $1, \omega, \omega^2$  are the cube roots of unity, then  $\frac{1}{1+2\omega} + \frac{1}{2+\omega} - \frac{1}{1+\omega} =$

1) 1

2)  $\omega$

3)  $\omega^2$

4) 0

11) The number of integral values of  $x$  satisfying  $5x - 1 < (x + 1)^2 < 7x - 3$  is

1) 0

2) 1

3) 2

4) 3

12) For real number  $x$ , if the minimum value of  $f(x) = x^2 + 2bx + 2c^2$  is greater than the maximum value of  $g(x) = -x^2 - 2cx + b^2$ , then

1)  $c^2 > 2b^2$

2)  $c^2 < 2b^2$

3)  $b^2 = 2c^2$

4)  $c^2 = 2b^2$

13) If  $a, b$  and  $c$  are the roots of  $x^3 + qx + r = 0$ , then  $(a - b)^2 + (b - c)^2 + (c - a)^2 =$

1)  $-6q$

2)  $-4q$

3)  $6q$

4)  $4q$

14) If the sum of two roots of the equation  $x^3 - 2px^2 + 3qx - 4r = 0$  is zero, then the value of  $r$  is

1)  $\frac{3pq}{2}$

2)  $\frac{3pq}{4}$

3)  $pq$

4)  $2pq$

15) The sum of the four digit even numbers that can be formed with the digits 0, 3, 5, 4 with out repetition is

1) 14684

2) 43536

3) 46526

4) 52336

16) If  $x$  is the number of ways in which six women and six men can be arranged to sit in a row such that no two women are together and if  $y$  is the number of ways they are seated around a table in the same manner, then  $x : y =$

1) 12 : 1

2) 42 : 1

3) 16 : 1

4) 6 : 1

17) The number of 5-letter words that can be formed by using the letters of the word SARANAM is

1) 1120

2) 6720

3) 480

4) 720

18) The number of rational terms in the binomial expansion of  $(\sqrt[4]{5} + \sqrt[5]{4})^{100}$  is

1) 50

2) 5

3) 6

4) 51

19) The numerically greatest term in the binomial expansion of  $(2a - 3b)^{19}$  when  $a = \frac{1}{4}$  and

$b = \frac{2}{3}$  is

1)  ${}^{19}C_5 \cdot 2^{11}$

2)  ${}^{19}C_3 \cdot \frac{1}{2^{11}}$

3)  ${}^{19}C_4 \cdot \frac{1}{2^{13}}$

4)  ${}^{19}C_3 \cdot 2^{13}$

20) If  $\frac{x^2 + 5x + 7}{(x-3)^3} = \frac{A}{(x-3)} + \frac{B}{(x-3)^2} + \frac{C}{(x-3)^3}$ , then the equation of the line having slope A and

Passing through the point (B, C) is

1)  $x + y - 20 = 0$

2)  $x - y + 20 = 0$

3)  $x + y + 20 = 0$

4)  $x - y - 20 = 0$

21) If  $\cos\left(x - \frac{\pi}{3}\right), \cos x, \cos\left(x + \frac{\pi}{3}\right)$  are in a harmonic progression, then  $\cos x =$

1)  $\frac{3}{2}$

2) 1

3)  $\frac{\sqrt{3}}{2}$

4)  $\sqrt{\frac{3}{2}}$

22)  $\cos^3 110^\circ + \cos^3 10^\circ + \cos^3 130^\circ =$

1)  $\frac{3}{4}$

2)  $\frac{3}{8}$

3)  $\frac{3\sqrt{3}}{8}$

4)  $\frac{3\sqrt{3}}{4}$

23) If the general solution of  $\sin 5x = \cos 2x$  is of the form  $a_n \cdot \frac{\pi}{2}$  for  $n = 0, \pm 1, \pm 2, \dots$ , then  $a_n =$

1)  $\frac{2n}{5+2(-1)^n}$

2)  $\frac{2n+(-1)^n}{5+2(-1)^n}$

3)  $\frac{2n+1}{5+2(-1)^n}$

4)  $\frac{2n-1}{5+2(-1)^n}$

24) Let  $x, y$  be real numbers such that  $x \neq y$  and  $xy \neq 1$ . If  $ax + b \sec(\tan^{-1}x) = c$  and  $ay + b \sec(\tan^{-1}y) = c$ , then  $\frac{x+y}{1-xy} =$

1)  $\frac{2ab}{a^2 - b^2}$

2)  $\frac{2ac}{a^2 + c^2}$

3)  $\frac{2ab}{a^2 + b^2}$

4)  $\frac{2ac}{a^2 - c^2}$

25)  $\tanh^{-1} \frac{1}{2} + \coth^{-1} 3 =$

1)  $\log \sqrt{6}$

2)  $\log 6$

3)  $-\log \sqrt{6}$

4)  $-\log 6$



26) If the median of a  $\Delta ABC$  through A is perpendicular to AC, then  $\frac{\tan A}{\tan C} =$

1)  $1 + \sqrt{2}$

2)  $-\frac{1}{\sqrt{3}} + 1$

3)  $-2$

4)  $1 + \frac{2}{\sqrt{3}}$

27) In  $\Delta ABC$ ,  $\tan \frac{A}{2} + \tan \frac{B}{2} =$

1)  $\frac{c \cot \frac{C}{2}}{4s}$

2)  $\frac{2c \cot \frac{C}{2}}{a+b+c}$

3)  $\frac{2c \tan \frac{C}{2}}{s}$

4)  $\frac{c \tan \frac{C}{2}}{a+b+c}$

28) In a  $\Delta ABC$ , D, E and F respectively are the points of contact of the incircle with the sides AB, BC and CA such that  $AD = \alpha$ ,  $BE = \beta$  and  $CF = \gamma$ , then  $\frac{\alpha\beta\gamma}{\alpha + \beta + \gamma} =$

1)  $R^2$

2)  $2R$

3)  $2r$

4)  $r^2$

29) Let  $\vec{a}, \vec{b}$  and  $\vec{c}$  be three non-coplanar vectors. The vector equation of a line which passes through the point of intersection of two lines, one joining the points  $\vec{a} + 2\vec{b} - 5\vec{c}$ ,  $-\vec{a} - 2\vec{b} - 3\vec{c}$  and the other joining the points  $-4\vec{c}$ ,  $6\vec{a} - 4\vec{b} + 4\vec{c}$  is

1)  $\vec{r} = 2\vec{a} - 4\vec{b} + 3\vec{c} + \mu(\vec{a} - 6\vec{b} + 4\vec{c})$

2)  $\vec{r} = 3\vec{a} + 6\vec{b} - \vec{c} + \mu(\vec{a} + 2\vec{b} + \vec{c})$

3)  $\vec{r} = 2\vec{a} + 3\vec{b} - \vec{c} + \mu(\vec{a} + \vec{b} - \vec{c})$

4)  $\vec{r} = 2\vec{b} + 3\vec{c} + \mu(\vec{a} - 4\vec{b} + 3\vec{c})$

30) In  $\Delta PQR$ , M is the mid-point of QR and C is the mid-point of PM. If QC when extended meets PR at N then  $\frac{|QN|}{|CN|} =$

1) 1

2) 2

3) 3

4) 4

31) If  $\vec{a} = \vec{i} - 2\vec{j} - 3\vec{k}$ ,  $\vec{b} = 2\vec{i} + \vec{j} - \vec{k}$ ,  $\vec{c} = \vec{i} + 3\vec{j} - 2\vec{k}$ , then  $[(\vec{a} \times \vec{b}) \times (\vec{b} \times \vec{c})(\vec{b} \times \vec{c}) \times (\vec{c} \times \vec{a})(\vec{c} \times \vec{a}) \times (\vec{a} \times \vec{b})] =$

1) 160000

2) -8000

3) 400

4) -40

32) If  $\vec{a} = \vec{i} + 2\vec{j} + 3\vec{k}$ ,  $\vec{b} = -\vec{i} + 2\vec{j} + \vec{k}$ ,  $\vec{c} = \vec{i} + 2\vec{j} - 2\vec{k}$ ,  $\vec{n}$  is perpendicular to both  $\vec{a}$  and  $\vec{b}$ , and  $\theta$  is the angle between  $\vec{c}$  and  $\vec{n}$  then  $\sin\theta =$

1)  $\frac{\sqrt{2}}{3}$

2)  $\frac{\sqrt{2}}{3\sqrt{3}}$

3)  $\frac{2}{\sqrt{3}}$

4)  $\frac{\sqrt{3}}{2}$

33) If  $\vec{a}, \vec{b}$  and  $\vec{c}$  are mutually perpendicular vectors of the same magnitude, then the cosine of the angle between  $\vec{a}$  and  $\vec{a} + \vec{b} + \vec{c}$  is

1)  $\frac{1}{\sqrt{2}}$

2)  $\frac{1}{\sqrt{3}}$

3)  $\frac{1}{2}$

4)  $\frac{\sqrt{3}}{2}$

34) If  $\vec{a}, \vec{b}$  and  $\vec{c}$  are non-coplanar vectors and the four points with position vectors  $2\vec{a} + 3\vec{b} - \vec{c}$ ,  $\vec{a} - 2\vec{b} + 3\vec{c}$ ,  $3\vec{a} + 4\vec{b} - 2\vec{c}$  and  $k\vec{a} - 6\vec{b} + 6\vec{c}$  are coplanar, then  $k =$

1) 0

2) 1

3) 2

4) 3

35)The mean and the standard deviation of a data of 8 items are 25 and 5 respectively. If two items 15 and 25 are added to this data, then the variance of the new data is

1)29

2)24

3)26

4) $\sqrt{29}$

36)The mean deviation from the median for the following distribution (corrected to two decimals) is

$x_i$	6	9	3	12	15	13	21	22
$f_i$	4	5	3	2	5	4	4	3

1)13.42

2)5.45

3)4.97

4)11.25

37)If a die is rolled three times, then the probability of getting a larger number on its face than the previous number each time, is

1) $\frac{15}{216}$

2) $\frac{5}{54}$

3) $\frac{13}{216}$

4) $\frac{1}{18}$

38) A man is known to speak the truth 2 out of 3 times. If he throws a die and reports that it is six, then the probability that it is actually five, is

1)  $\frac{3}{8}$

2)  $\frac{1}{7}$

3)  $\frac{2}{7}$

4)  $\frac{4}{5}$

39) If the probability function of a random variable X is defined by  $P(X = k) = a \left( \frac{K+1}{2^k} \right)$  for  $k = 0, 1, 2, 3, 4, 5$  then the probability that X takes a prime value is

1)  $\frac{13}{20}$

2)  $\frac{23}{60}$

3)  $\frac{11}{20}$

4)  $\frac{19}{60}$

40) If X is a binomial variate with mean 6 and variance 2, then the value of  $P(5 \leq X \leq 7)$  is

1)  $\frac{4762}{6561}$

2)  $\frac{4672}{6561}$

3)  $\frac{5264}{6561}$

4)  $\frac{5462}{6651}$

41) Let A(2, 3), B(3, -6), C(5, -7) be three points. If P is a point satisfying the condition  $PA^2 + PB^2 = 2PC^2$ , then a point that lies on the locus of P is

1)(2, -5)

2)(-2, 5)

3)(13, 10)

4)(-13, -10)

42) If the coordinates of a point P changes to (2, -6) when the coordinate axes are rotated through an angle of  $135^\circ$ , then the coordinates of P in the original system are

1)(-2, 6)

2)(-6, 2)

3)( $2\sqrt{2}$ ,  $4\sqrt{2}$ )

4)( $\sqrt{2}$ ,  $-\sqrt{2}$ )

43) If the portion of a line intercepted between the coordinate axes is divided by the point (2, -1) in the ratio 3 : 2, then the equation of that line is

1)  $5x - 2y - 20 = 0$

2)  $2x - y - 5 = 0$

3)  $3x - y - 7 = 0$

4)  $x - 3y - 5 = 0$

44) The equation of the line passing through the point of intersection of the lines  $2x + y - 4 = 0$ ,  $x - 3y + 5 = 0$  and lying at a distance of  $\sqrt{5}$  units from the origin, is

1)  $x - 2y - 5 = 0$

2)  $x + 2y - 5 = 0$

3)  $x + 2y + 5 = 0$

4)  $x - 2y + 5 = 0$

45) The equation of the line joining the centroid with the orthocentre of the triangle formed by the points  $(-2, 3)$ ,  $(2, -1)$ ,  $(4, 0)$  is

1)  $x + y - 20 = 0$

2)  $11x - y - 14 = 0$

3)  $x - 11y + 6 = 0$

4)  $2x - y - 2 = 0$

46) The lines represented by the equations  $23x^2 - 48xy + 3y^2 = 0$  and  $2x + 3y + 4 = 0$  form

1) an isosceles triangle

2) a right angled triangle

3) an equilateral triangle

4) a scalene triangle

47) If the line  $x + 2y = k$  intersects the curve  $x^2 - xy + y^2 + 3x + 3y - 2 = 0$  at two points A and B and if O is the origin, then the condition for  $\angle AOB = 90^\circ$  is

1)  $k^2 + k + 1 = 0$

2)  $k^2 - 2k + 1 = 0$

3)  $2k^2 + 9k - 10 = 0$

4)  $3k^2 + 8k - 1 = 0$

48) If  $2x^2 + 3xy - 2y^2 = 0$  represents two sides of a parallelogram and  $3x + y + 1 = 0$  is one of its diagonals, then the other diagonal is

1)  $x - 3y + 1 = 0$

2)  $x - 3y + 2 = 0$

3)  $x - 3y = 0$

4)  $3x - y = 0$

49) If the lengths of the tangents drawn from P to the circles  $x^2 + y^2 - 2x + 4y - 20 = 0$  and  $x^2 + y^2 - 2x - 8y + 1 = 0$  are in the ratio 2:1, then the locus of P is

1)  $x^2 + y^2 + 2x + 12y + 8 = 0$

2)  $x^2 + y^2 - 2x + 12y + 8 = 0$

3)  $x^2 + y^2 + 2x - 12y + 8 = 0$

4)  $x^2 + y^2 - 2x - 12y + 8 = 0$

50) The equation of a circle touching the coordinate axes and the line  $3x - 4y = 12$  is

1)  $x^2 + y^2 + 6x + 6y + 9 = 0$

2)  $x^2 + y^2 + 6x + 6y - 9 = 0$

3)  $x^2 + y^2 - 6x - 6y + 9 = 0$

4)  $x^2 + y^2 - 6x - 6y - 9 = 0$

51) The pole of the straight line  $9x + y - 28 = 0$  with respect to the circle  $2x^2 + 2y^2 - 3x + 5y - 7 = 0$  is

1) (3, 1)

2) (3, -1)

3) (-3, 1)

4) (4, -8)

52) The point of intersection of the direct common tangents drawn to the circles  $(x + 11)^2 + (y - 2)^2 = 225$  and  $(x - 11)^2 + (y + 2)^2 = 25$  is

1)  $\left(\frac{-11}{2}, 1\right)$

2) (-22, 4)

3)  $\left(\frac{11}{2}, -1\right)$

4) (22, -4)



53) In List-I, a pair of circles is given in A, B, C and in List-II, angle between those pair of circles is given. Match the items from List-I to List-II.

**List-I**

A)  $(x - 2)^2 + y^2 = 2$

$(x - 2)^2 + (y - 1)^2 = 1$

B)  $x^2 + y^2 - 6x - 6y + 9 = 0$

$x^2 + y^2 - 4x + 4y - 9 = 0$

C)  $x^2 + y^2 + 4x - 14y + 28 = 0$

$x^2 + y^2 + 4x - 5 = 0$

**List-II**

I)  $90^\circ$

II)  $135^\circ$

III)  $60^\circ$

iv)  $30^\circ$

The correct matching is

1) A-I, B-II, C-III

2) A-II, B-I, C-III

3) A-III, B-I, C-IV

4) A-IV, B-III, C-I

54) If the radical axis of the circles  $x^2 + y^2 + 2gx + 2fy + c = 0$  and  $2x^2 + 2y^2 + 3x + 8y + 2c = 0$  touches the circle  $x^2 + y^2 + 2x + 2y + 1 = 0$ , then

1)  $g = \frac{3}{4}$  or  $f = 2$

2)  $g \neq \frac{3}{4}$ ,  $f = 2$

3)  $g = \frac{3}{4}$ ,  $f \neq 2$

4)  $g = \frac{2}{5}$  or  $f = 1$

55) The line  $y = 6x + 1$  touches the parabola  $y^2 = 24x$ . The coordinates of a point P on this line from which the tangent to  $y^2 = 24x$  is perpendicular to the line  $y = 6x + 1$ , is

1)  $(-1, -5)$

2)  $(-2, -11)$

3)  $(-6, -35)$

4)  $(-7, -41)$

56) A point on the parabola whose focus is S(1, -1) and whose vertex is A(1, 1) is

1)  $\left(3, \frac{1}{2}\right)$

2)  $(1, 2)$

3)  $\left(2, \frac{1}{2}\right)$

4)  $(2, 2)$

57) An ellipse having the coordinate axes as its axes and its major axis along Y-axis, passes through the point  $(-3, 1)$  and has eccentricity  $\sqrt{\frac{2}{5}}$ . Then its equation is

1)  $3x^2 + 5y^2 - 15 = 0$

2)  $5x^2 + 3y^2 - 32 = 0$

3)  $3x^2 + 5y^2 - 32 = 0$

4)  $5x^2 + 3y^2 - 48 = 0$

58) The product of the perpendicular distances drawn from the points (3, 0) and (-3, 0) to the tangent of the ellipse  $\frac{x^2}{36} + \frac{y^2}{27} = 1$  at  $\left(3, \frac{9}{2}\right)$  is

1) 36

2) 27

3) 9

4) 63

59) The equation of the hyperbola whose asymptotes are the lines  $3x + 4y - 2 = 0$ ,  $2x + y + 1 = 0$  and which passes through the point (1, 1) is

1)  $6x^2 + 11xy + 4y^2 - 30x + 2y + 7 = 0$

2)  $6x^2 + 11xy + 4y^2 - x + 2y - 22 = 0$

3)  $6x^2 + 11xy + 4y^2 - x + 2y + 22 = 0$

4)  $6x^2 + 11xy + 4y^2 - 3x - 7y - 11 = 0$

60) If the orthocentre and the centroid of a triangle are (-3, 5, 2) and (3, 3, 4) respectively, then its circumcentre is

1) (6, 2, 5)

2) (6, 2, -5)

3) (6, -2, 5)

4) (6, -2, -5)

61) A Plane cuts the coordinate axes X, Y, Z at A, B, C respectively such that the centroid of the  $\Delta ABC$  is (6, 6, 3). Then the equation of that plane is

1)  $x + y + z - 6 = 0$

2)  $x + 2y + z - 18 = 0$

3)  $2x + y + z - 18 = 0$

4)  $x + y + 2z - 18 = 0$

62) If the foot of the perpendicular drawn from the origin to a plane is (1, 2, 3), then a point on that plane is

1) (3, 2, 1)

2) (7, 2, 1)

3) (7, 3, -1)

4) (6, -3, 4)

63) If  $[x]$  denotes the greatest integer  $\leq x$ , then

$$\lim_{n \rightarrow \infty} \frac{1}{n^3} \{ [1^2 x] + [2^2 x] + [3^2 x] + \dots + [n^2 x] \} =$$

1)  $\frac{x}{2}$

2)  $\frac{x}{3}$

3)  $\frac{x}{6}$

4) 0

64) If a function  $f$  defined by  $f(x) = \begin{cases} \frac{1-\sqrt{2}\sin x}{\pi-4x}, & \text{if } x \neq \frac{\pi}{4} \\ k & , \text{if } x = \frac{\pi}{4} \end{cases}$

is continuous at  $x = \frac{\pi}{4}$ , then  $k =$

1)  $\frac{1}{4}$

2) 1

3)  $\frac{-1}{4}$

4) 2

65) The derivative of  $f(x) = x^{\tan^{-1}x}$  with respect to  $g(x) = \sec^{-1}\left(\frac{1}{2x^2-1}\right)$  is

1)  $\frac{1}{2}\sqrt{1-x^2}x^{\tan^{-1}x}\left[\frac{\log x}{1+x^2} + \frac{\tan^{-1}x}{x}\right]$

2)  $-\frac{1}{2}\sqrt{1-x^2}x^{\tan^{-1}x}\left[\log(\tan^{-1}x) + x(1+x^2)\tan^{-1}x\right]$

3)  $\frac{-2\tan^{-1}x\left[\frac{\log x}{1+x^2} + \frac{\tan^{-1}x}{x}\right]}{\sqrt{1-x^2}}$

4)  $-\frac{1}{2}\sqrt{1-x^2}x^{\tan^{-1}x}\left[\frac{\log x}{1+x^2} + \frac{\tan^{-1}x}{x}\right]$

66) If  $x = 3\cos t$  and  $y = 4\sin t$ , then  $\frac{d^2y}{dx^2}$  at the point  $(x_0, y_0) = \left(\frac{3}{2}\sqrt{2}, 2\sqrt{2}\right)$ , is

1)  $\frac{4\sqrt{2}}{9}$

2)  $-\frac{4\sqrt{2}}{9}$

3)  $\frac{8\sqrt{2}}{9}$

4)  $-\frac{8\sqrt{2}}{9}$

67) If  $y = \frac{2}{\sqrt{a^2 - b^2}} \tan^{-1} \left[ \sqrt{\frac{a-b}{a+b}} \tan \frac{x}{2} \right]$ , then  $\frac{d^2y}{dx^2} \Big|_{x=\frac{\pi}{2}} =$

1)  $\frac{b}{2a^2}$

2)  $\frac{b}{a^2}$

3)  $\frac{2b}{a}$

4)  $\frac{b^2}{2a}$

68) If  $f(x) = x^3 + ax^2 + bx + 5\sin^2 x$  is an increasing function on  $\mathbb{R}$ , then

1)  $a^2 - 3b - 15 < 0$

2)  $a^2 - 3b + 15 > 0$

3)  $a^2 - 3b - 15 > 0$

4)  $a^2 + 3b + 15 > 0$

69) The approximate value of  $\cos 31^\circ$  is (Take  $1^\circ = 0.0174$ )

1) 0.7521

2) 0.866

3) 0.7146

4) 0.8573

70) If  $x$  and  $y$  are two positive numbers such that  $x + y = 32$ , then the minimum value of  $x^2 + y^2$  is,

1) 500

2) 256

3) 1024

4) 512

71) The constant 'c' of Lagrange's mean value theorem for the function  $f(x) = \frac{2x+3}{4x-1}$  defined on  $[1, 2]$  is

1)  $\frac{1+\sqrt{15}}{3}$

2)  $\frac{1+\sqrt{21}}{4}$

3)  $\frac{5}{3}$

4)  $\frac{3}{2}$

72)  $\int \frac{\sin 2x dx}{\sin^4 x + \cos^4 x} = \tan^{-1}(f(x)) + c$ , then  $f\left(\frac{\pi}{3}\right) =$

1) 1

2) 2

3) 3

4)  $\frac{1}{3}$

$$73) \int \left( \frac{\log x - 1}{1 + (\log x)^2} \right)^2 dx =$$

1)  $\frac{\log x}{1 + (\log x)^2} + c$

2)  $\frac{x}{x^2 + 1} + c$

3)  $\frac{x}{1 + (\log x)^2} + c$

4)  $\frac{-x}{1 + (\log x)^2} + c$

$$74) \int \frac{dx}{x^3 + 3x^2 + 2x} =$$

1)  $\log|x| + \log\left|\frac{x+2}{x+1}\right| + c$

2)  $\log|x| - \log|x+1| + \log|x+2| + c$

3)  $\frac{1}{2} [\log|x| + \log|x+1| + \log|x+2|] + c$

4)  $\frac{1}{2} \log\left(\frac{|x^2 + 2x|}{(x+1)^2}\right) + c$



75) For  $n \geq 2$ , If  $I_n = \int \sec^n x dx$ , then  $I_4 - \frac{2}{3}I_2 =$

1)  $\sec^2 x \tan x + c$

2)  $\frac{1}{3} \sec^2 x \tan x + c$

3)  $\frac{2}{3} \sec^2 x \tan x + c$

4)  $\frac{1}{3} \log |\sec x + \tan x| + c$

76)  $\lim_{n \rightarrow \infty} \left( \frac{\sqrt{1} + 2\sqrt{2} + 3\sqrt{3} + \dots + n\sqrt{n}}{n^{\frac{5}{2}}} \right) =$

1) 1

2)  $\frac{5}{2}$

3) 0

4)  $\frac{2}{5}$

77)  $\int_0^{\frac{\alpha}{3}} \frac{f(x)}{f(x) + f\left(\frac{\alpha - 3x}{3}\right)} dx =$

1)  $\frac{2\alpha}{3}$

2)  $\frac{\alpha}{2}$

3)  $\frac{\alpha}{3}$

4)  $\frac{\alpha}{6}$

78) The area (in sq. units) of the region bounded by the X-axis and the curve  $y = 1 - x - 6x^2$  is

1)  $\frac{125}{216}$

2)  $\frac{125}{512}$

3)  $\frac{25}{216}$

4)  $\frac{25}{512}$

79) If  $m$  and  $n$  are respectively the order and degree of the differential equation of the family of parabolas with focus at the origin and X-axis as its axis, then  $mn - m + n =$

1) 1

2) 4

3) 3

4) 2

80) The general solution of  $\left(1 + e^{\frac{x}{y}}\right) dx + e^{\frac{x}{y}} \left(1 - \frac{x}{y}\right) dy = 0$  is

1)  $ye^x + x = c$

2)  $ye^y - x = c$

3)  $ye^y + y = c$

4)  $ye^y + x = c$

APEAMCET-2018 -- Engineering Stream			
Final Key			
Date: 22-04-18 FN (Shift 1)			
1	4	41	4
2	4	42	3
3	4	43	4
4	3	44	2
5	4	45	2
6	1	46	3
7	4	47	3
8	1	48	3
9	4	49	4
10	4	50	3
11	2	51	2
12	1	52	4
13	1	53	2
14	1	54	1
15	2	55	3
16	2	56	1
17	3	57	4
18	3	58	2
19	4	59	2
20	2	60	1
21	4	61	4
22	3	62	2
23	2	63	2
24	4	64	1
25	1	65	4
26	3	66	4
27	2	67	2
28	4	68	1
29	2	69	4
30	4	70	4
31	1	71	2
32	2	72	3
33	2	73	3
34	2	74	4
35	1	75	2
36	3	76	4
37	2	77	4
38	2	78	1
39	2	79	3
40	2	80	4